

The Reflectivity Tool

# THE MANUAL

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# Contents





# <span id="page-3-3"></span><span id="page-3-0"></span>1 Introduction

This manual briefly explains the use of PARRATT32. Most aspects are covered also by the on–line help accessible from within the programme. This document's purpose is to be printed out and to be read separately while or before working with the programme. It also serves as a source of reference in cases where users get stuck with some sort of problem. The second part of the manual describes the vital parts of the source code and gives a brief summary of how to compile it to get the executable. On the screen some of the graphics in this documentation might look ugly, but once printed out the quality increases.

# <span id="page-3-1"></span>2 The Programme

PARRATT32 is a programme to calculate the optical reflectivity of neutrons or x-rays from flat surfaces. The calculation is based on Parratt's recursion scheme for stratified media [\[Parratt54\]](#page-27-1). PARRATT32 is a Microsoft Windows application (either Windows 95, Windows 98 or Windows NT 4.0 — the i386 edition works fine, other platforms, such as FX32 on DEC Alpha could not be tested). The 32 bit extensions for 16bit-Windows (versions 3.1x, also known as Win32s) are not sufficient!

## <span id="page-3-2"></span>2.1 The Graphical User Interface



PARRATT32's graphical user interface (GUI for short, or main window) is shown in figure [2.1.](#page-3-2) The main elements, depicted by the arrows are described in the next sections.

## <span id="page-4-0"></span>2.1.1 Menu Bar

The Menu Bar. In the menu bar the different menu entries can be selected with the mouse or with key strokes. Most of the functionality that PARRATT32 delivers can be found here.

## 2.1.2 Tool Bar

Some of the frequently used items from the menu have The Tool Bar. short–cuts placed in the tool bar as little buttons. This makes accessing these items with the pointing device (i.e. the mouse) very handy.

## 2.1.3 Reflectivity Window

This window is for displaying the reflectivity  $(R \text{ vs.}$  $Q<sub>z</sub>$ ) calculated from the given sample. Measured sets of data that were loaded into the programme are displayed here, too.

## 2.1.4 Profile Window

From the data given in the model window a scattering length density profile can be calculated. The resulting  $\rho$  vs. z is displayed in this window.

#### 2.1.5 Model Window

The model window is the place where the most relevant information of the model sample is stored. Mainly this is a description of how the scattering length density varies with the different layers that make up the sample.

#### 2.1.6 Status Bar

Important programme information is displayed here The Status Bar. from time to time, i. e. moving the mouse pointer in one of the graphics windows will display the respective coordinates.

## 2.1.7 Copyright Notification Area

This tool bar is just a reminder of where you got the Copyright Notification Area. software from and who paid for it...



File Edit Calculate Database Window Help

 $Qz = 0.2500; R = 2.211E-06$ 



# <span id="page-5-3"></span><span id="page-5-0"></span>3 Working with the Programme

## <span id="page-5-1"></span>3.1 Loading Data

The only kind of data PARRATT32 can handle is ASCII files made up of three or more columns separated by a TAB character (ASCII 9). The first column are the  $Q_z$ values, the second column are the  $R(Q_z)$  values (where  $R(0) \equiv 1$ ) and the third column are  $\delta R(Q_z)$ . These can be set to zero. Additional columns will be ignored. Since the reflectivity plot is logarithmic, Par-RATT32 will ignore negative values in the second column. There is some error handling routine, that lets PARRATT32 ignore certain lines in the file: i.e. header lines, negative  $R$ 's or other kind of NANs. Once finished loading the data, it will be displayed as small green circles in the reflectivity window.

## <span id="page-5-2"></span>3.2 Setting up a Model

On start–up PARRATT32 loads a standard set of parameters. Some of these parameters will be stored in the Window's registry when you end working with the programme and will be reloaded the next time you start PARRATT32. In the model window the basic sample start–up parameters are always Si bulk material with a  $25 \text{ Å } SiO_2$  layer on top of it (values for  $4.66$  Å neutrons).

Prior to fitting a model for the layer system has to be set up. There are three basically different sample types in PARRATT32 which will be described in the next sections. For every layer in the model at least two values have to be entered, four more can be entered. The two essential values are: the layer thickness in Ångstrøm  $(d/\text{\AA})$  and the real part of the scattering length density  $(rh\omega/\text{\AA}^{\sim}-2)$ . The four optional parameters are the imaginary part of the scattering length density  $(Im(rho/\text{Å}^{\text{-}}-2))$ , the roughness of the layer  $(sigma/A)$ , and the magnetic contribution to the scattering length density  $(R(\text{mag}), I(\text{mag}), \text{same units as})$ rho and Im(rho)).

<span id="page-6-0"></span>

A simple model is made up of a varying number of essentially different layers. By selecting the radio button labeled "independent layers" the model window rearranges to its most simple form: there is only one edit field for the number of layers and below it is shown a table where one wants to type in the respective properties for the layers. By changing the number of layers in the edit field one can change the number of rows in the table. Up to four hundred layers can make up such a simple sample, but who wants to type in these values...



independent layer mode

#### 3.2.2 Models With Functions

Sometimes it might be useful to describe the scattering length density profile of interfaces by analytical functions. By pressing the "edit function" button a dialogue shows up where a function can either be chosen from a list of predefined ones or typed as an expression. The latter, so called user–functions, can also be saved to file and reloaded later on. PARRATT32 comes with four built–in functions: exponential decay, Liu– Fisher decay [\[Liu89\]](#page-27-2), oscillating, and oscillating with decaying amplitude.

These function are hard–coded, so the evaluation of the scattering length density is fast, and so is the calculation of the reflectivity, well, at least faster than for the user–functions, that run through the function parser each time a value is requested. Apart from choosing the function there are other parameters to be set in the model. Firstly, the layers between which the functional expression is inserted has to be specified. This can be done in the edit field labeled "append function to layer No.". Append means when you choose 1, the function will be appended to layer one, which is between layer one and two! Secondly, the range of the function with respect to the  $z$ -coordinate must be given. This is done with the two edit fields "thickness..." and "number of steps", which, by multiplying give the total depth of the region between the chosen layers. For convenience, there is a button labeled "I want to test my function" which calculates the reflec-



profile function mode



The function edit dialogue

<span id="page-7-1"></span>tivity and the profile.

#### 3.2.3 Multi Layer Models

Often samples come with regularly arranged stacks of layers, so called multi–layered systems. To handle these more conveniently the model window can be switch to multi–layer mode. Here a second table shows up: the multi–layer stack. This stack, which behaves in the same way as does the basic sample, can be inserted into the basic sample at an arbitrary position (edit field "append multi layer..."). This means one can have layers of the basic sample above the multi– layer stack and below it. The multi–layer stack itself consists of at least two different materials (edit field "number of layers in the stack"), which can be repeated several times (edit field "number of repetitions"). The total thickness of the sample is then calculated from the thickness of the basic sample plus the thickness of the multi–layer stack multiplied by the number of repetitions.

#### <span id="page-7-0"></span>3.3 Calculating the Reflectivity

The reflectivity  $R(Q_z)$  of the model can be displayed by either selecting "Calculate–Reflectivity" from the main menu or by pressing the calculator button  $\blacksquare$  in the tool bar. Note: the tool bar shows so called tool tips if the mouse pointer rests over he images for a little while. After a short while — depending of the speed of the computer and the complexity of the model — the calculation will be finished and the reflectivity curve will be displayed in the reflectivity window. The scaling of the graph is done automatically.

	<b>Model</b>					
	sample type:	C. multiple layers	C independent layers analytical profile function			
		number of layers: $\boxed{1}$				
		number of layers $\sqrt{2}$	number of $\boxed{1 + \frac{1}{2}}$ append multilayer $\boxed{0 + \frac{1}{2}}$			
	$d/\text{Å}$ 50	rho / Å^-2 8e-6	Im(rho) / Å^-2 sigma / Å n	n	R(mag) n	I(mag) n
	11	5e-7	n	n	n	n
	d/Å		rho / Å^-2   Im(rho) / Å^-2   sigma / Å		R(mag)	I(mag)
	N/A	n	n	N/A	O	O
No. $\overline{\mathcal{L}}$ air	25	3.475E-6	1.05E-11	n	n	n

multi–layer mode



## <span id="page-8-2"></span><span id="page-8-0"></span>3.4 Calculating SLD Profiles

The scattering length density profile  $\rho(z)$  of the sample can be calculated by either selecting "Calculate– Profile" from the main menu or by pressing the profile button  $\mathbf{r}$  in the tool bar. The progress of the calculation is displayed in the programme's status bar. After the calculation is done the resulting scattering length density profile is displayed in the profile window, which also rescales automatically.

By simultaneously pressing the shift key, the left mouse button, and dragging the mouse a rectangle can be drawn inside the graph windows. This rectangle then defines the new minimal and maximal coordinates of the diagram. For automatic rescaling simply hold shift and press the left mouse button somewhere inside the window, hopefully everything will return to normal.

## <span id="page-8-1"></span>3.5 Setting Various Calculation Parameters

Most calculation relevant settings are accessible via the "Settings Dialogue". It will be shown when selecting "Calculate–Settings" from the main menu. The dialogue box comes with a lot of pages which will be explained in the next sections. On the bottom of the box there are four buttons three of which have the standard meaning ("Ok", "Cancel", and "Help") but the fourth  $\blacksquare$  calculates either the reflectivity or the profile depending on what page is selected in the dialogue.

#### 3.5.1 Reflectivity Calculation Settings

On the first page of the dialogue box the settings for reflectivity calculation can be specified. The wavelength edit field is only relevant, when inserting values from the scattering length density database in the model window.

When the chackbox labeled "user supplied Q–range" is checked the reflectivity will be calculated according to the values given in the edit fields. Unchecking the box will disable these fields and either set the values to the default ones or to the values found in the data file.







<span id="page-9-0"></span>When the checkbox labeled "include magnetization" is checked, the reflectivity will be calculated for three different models:

a)  $R(Q_z)$  from the *ordinary* values in the model file  $(rho \text{ and } Im(rho)).$ 

b)  $R^+(Q_z)$  from rho+ R(mag) and Im(rho)+I(mag),

c)  $R^{-}(Q_z)$  from rho-R(mag) and Im(rho)- I(mag).

The three calculations can be distinguished by their different colour in the reflectivity window:

 $R$  is plotted **black** 

 $R^+$  is plotted red

 $R^-$  is plotted **blue** 

#### 3.5.2 Transmission Calculation Settings

For *free* samples, i.e. where the substrate is not infinitely thick on a macroscopic scale, the intensity of the transmitted radiation can be calculated. The calculation is mainly based on the length of the path the radiation travels through the substrate. Therefore the substrate's thickness has to be specified (in millimeters). Also, the wavelength of the incident radiation has to be specified (this is done on the "Reflectivity Settings"–page) since the absorption cross section of the substrate's material is corrected for the wavelength.

#### 3.5.3 Profile Calculation Settings

The range of the calculation of the scattering length density profile can be set by checking the box marked "user supplied z–range". This will enable the edit fields, so that values may be entered for the lower and upper boundary as well as for the number of steps on the  $z$ -Axis. Unchecking this box will result in an automatic recalculation of the minimum and maximum setting for the  $z$ -range depending on the thicknesses given in the model window. For a single air/bulk interface the default values are -25 Å to +25 Å for samples with  $N_{\text{layer}} \geq 1$  the calculation will range from  $-25\%$  to  $+25\%$  of the overall sample thickness. The overall sample thickness is calculated from all layers of the given model including the functional region of the model or the including the multi layer stack. In





<span id="page-10-0"></span>the case of multi layer or function models the default number of points where the scattering length is calculated (one hundred) can get too small to virtually see all features of the profile. In this case one is advised to manually choose the calculation region.

#### 3.5.4 Background Settings

Working with real data often involves reflectivities measured down to a certain noise limit, which is also known as instrumental background. In the case of uncorrected data, which is, no background substracted from the raw data, this background can be added to the calculated reflectivity. PARRATT32 offers different types of background noise to be added to the data: a) the typical noise threshold of the reflectivity instrument (constant  $y_0$ ), b) linear increasing or decreasing background characterized by a constant  $y_0$  and a slope  $m$ , c) and d) peaking background (either of gaussian or lorentzian shape) on a baseline that is characterized by five values:  $y_0$  and m for the baseline and A, w, and  $x_c$  for the area, the width, and the center position of the peak.



#### 3.5.5 Resolution Settings

Real reflectometers all have a finite angular resolution. This means that measured  $R(Q_z)$ –values are virtually  $R(Q_z \pm \delta Q_z)$  values. PARRATT32 can approximate this resolution by calculating the reflectivity at a position  $Q<sub>z</sub>$  plus gaussian weighted reflectivities at eight additional positions  $Q_z \pm \delta Q_z$ ,  $Q_z \pm 3\delta Q_z/4$ ,  $Q_z \pm \delta Q_z/2$ , and  $Q_z \pm \delta Q_z/4$ . Due to a lack of incoming radiation reflectivity curves are sometimes measured with different resolutions in different  $Q_z$  regimes, i.e. different settings of the collimation system. Therefore up to eight regions with different resolutions can be specified in the dialogue's resolution table. The first column is the starting value of the  $Q_z$ -region — which obviously should be zero in the first row  $-$ , the second column is the  $\delta Q_z$ . Some neutron reflectometers use a velocity selector instead of a crystalline monochromator. The wavelength distribution  $(\Delta\lambda/\lambda)$  such a device is constant, hence the resolution decreases with increasing





<span id="page-11-1"></span>in  $Q_z$ . Clicking the velocity selector checkbox allows you to enter the appropriate values.

#### 3.5.6 The SLD Database Settings

There is a handy way to fill in the values for the different layers in the model window. By clicking with the right mouse button on the first column of a row in the model window a small pop–up menu will appear. Now, element's or compound's properties can be selected to be put into the respective row's rho and Im(rho) column. These values are taken from a database that PARRATT32 loads at programme start– up. To correctly insert the values into the model window, the radiation type (neutrons or x–rays) has to be specified. For details on the database see below.

#### <span id="page-11-0"></span>3.6 Fitting Models to Data

Once data is loaded and an appropriate model is set up, this model can then be fitted to the experimental data. By either selecting "Calculate–fit data" or by pressing the fit–button  $\vert \mathbf{E} \vert$  from the tool bar the FitIt dialogue box will show up. This dialogue box comes with two pages.

On page one three main elements can be found: the list of parameters, the  $\chi^2$  label and the *fitting control* center. Selecting the parameters is simply done by clicking on the checkbox next to it. All values of the parameters that are marked will be varied during the fitting procedure. The  $\chi^2$  label shows the momentary goodness–of–fit during the procedure. In the fitting control center one can either select a single  $\chi^2$  evaluation with the values of parameters given in the list or a complete minimization run with the selected parameters. The tolerance value given in the edit field is read out every time a new  $\chi^2$  was calculated. Convergence of a single parameter is reached when the following expression is satisfied:  $|\chi^2_{old} - \chi^2_{new}|$  ≤tolerance. Once the "do it"–button is pressed, the calculation is under way. The progress of the calculation can be monitored in PARRATT32's status bar. The first num-

ber given there is the number of the parameter which is currently varied, the second number is the current





Page 1 of the FitIt dialogue box



<span id="page-12-0"></span>iteration step. The fitting procedure can be stopped by pressing the button labeled "stop".

Some fitting related settings can be made on page two of the FitIt dialogue box. At first the weighting of the  $\chi^2$  calculation has to be chosen. Additionally, one can include the background and resolution settings from the "Settings Dialogue" into the fit procedure.

## 3.6.1 Defining a Fitting Region

A fitting region can be defined in the reflectivity window by the following procedure: Data has to be loaded, mark the left border of the region (low  $Q$ ) by holding down the control key (Ctrl) and press the left mouse button when the mouse pointer is in the vicinity of the leftmost datapoint of the desired region. The corresponding data point will turn black! Now hold down Ctrl again and press the right mouse button on the rightmost datapoint. A message will pop up to tell about the region in  $Q_z$  that was selected. Once fitting is done the region is discarded and the reflectivity is calculated for the whole dataset again.

Page 2 of the FitIt dialogue box



## <span id="page-13-2"></span><span id="page-13-0"></span>3.7 Saving the Results

The data of all three windows can be saved to file. In the file menu there are entries for saving the data of each window. One can also use the save button from the tool bar  $\Box$  which then saves the contents of the currently active window (the one, which has the highlighted title bar).

The data from the model window will be saved in a special PARRATT32 format, which contains all the layer information plus the background and resolution settings from the settings dialogue.

The data from the profile window will be saved as two– column ASCII, with the first column as  $z/\text{\AA}$  and the second column as  $\varrho/\AA^{-2}$ .

The data of the reflectivity window depends on the magnetization and transmission settings. If none of these is selected the data will be saved as three TAB– delimited column ASCII files: column one are the  $Q<sub>z</sub>$ -values, column two are the calculated reflectivity values and column three are zeros. If "include magnetization" is checked in the "settings dialogue box" then the file will be expanded to five columns, the last two containing  $R^+(Q_z)$  and  $R^-(Q_z)$ . If "calculate transmission" is checked in the "settings dialogue box" then the file will expand to four columns, the fourth column containing the  $T(Q_z)$  values. If both are checked, then there will be six columns in the file:  $Q_z, R, 0, R^+, R^-, T$ .

#### <span id="page-13-1"></span>3.8 Copying Data

Since PARRATT32's graphical features are limited data from both the reflectivity window and the profile window can be copied to the Window's clipboard and pasted to other Windows applications, such as spreadsheet or scientific graphic applications  $(i. e. Excel or$ Origin).

Copying the data from the profile window results in a two column dataset: z and  $\rho(z)$ .

Copying the data from the reflectivity window leaves you with at least two columns in the clipboard: Q and  $R(Q)$ . If you selected to include the calculation of the transmission of the sample, then there Some examples for the different file formats of calculated reflectivity data: a) bare reflectivit

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<span id="page-14-1"></span>will be three columns:  $Q, R(Q)$ , and  $T$ . If magnetization is included, then there will be four columns:  $Q, R(Q), R^+(Q)$ , and  $R^-(Q)$ . And finally, if transmission and magnetization are included then there are five columns:  $Q, R(Q), R^+(Q), R^-(Q)$ , and T.

#### <span id="page-14-0"></span>3.9 Printing the Results

For a quick–and–dirty overview of the results from a fitting session one can print out a summary sheet. Either selecting "File-Print..." or clicking the printer button  $\blacksquare$  from the tool bar will launch Windows' standard printing dialogue to select the printing device. Best results are achieved on A4 sized paper, but letter size will also work.



## <span id="page-15-0"></span>4 Some Internals

## <span id="page-15-1"></span>4.1 The SLD Database

PARRATT32 comes with a user expandable material's properties database. By default the relevant files are located in <installdir>/database/. The main file (Parratt32.db) is a Paradox7 table. This table can be edited via "Database–edit" from the main menu. The index files — files that provide the sorting order of the table — are automatically regenerated when new entries are send to the database. Elements are sorted according to the periodic system, compounds are sorted by name. From the values given in the database table PARRATT32 calculates the values rho and  $Im(rho)$  according to the following formulae:

neutrons: 
$$
V[\text{\AA}^3] = \frac{M[\text{g/mol}]}{\rho_{\text{mass}}[\text{g/cm}^3] \cdot N_{\text{A}}[\text{mol}^{-1}]} \cdot 10^{24}
$$

$$
\rho[\text{\AA}^{-2}] = \frac{b_{\text{coh}}[\text{fm}]}{V[\text{\AA}^3]} \cdot 10^{-5}
$$

$$
Im(\rho)[\text{\AA}^{-2}] = \frac{\text{abs} \cdot \text{xs}[\text{barn}]}{1.789[\text{\AA}] \cdot 2 \cdot V[\text{\AA}^3]} \cdot 10^{-8}
$$

$$
\text{x-rays:} \qquad \rho[\text{\AA}^{-2}] = \frac{2\pi\delta}{1.541^2}
$$

$$
Im(\rho)[\text{\AA}^{-2}] = \frac{2\pi\beta}{1.541 \cdot \lambda}
$$

Note: 1.789 Å  $(2200 \text{m/s})$  is the wavelength for which the absorption cross section values are tabulated, and 1.541 Å (Cu–K<sub>α</sub>, 8047 eV) is the wavelength for which the  $\delta$  and  $\beta$  values are supplied in the table.

## <span id="page-15-2"></span>4.2 Hidden Features

## 4.2.1 Command Line Parameters

For faster loading PARRATT32 can be started without the database file being loaded: simply type "parratt nodatabase" in the programme's directory, without the quotes, of course. The database file can then be loaded later on by selecting "Database-load from disk" from the main menu. Also, if you don't like the welcome screen simply type "parratt nosplash". Both of these parameters can be specified in the properties dialog of the shortcut placed in the Start menu by the installation procedure, see the Windows help for details...

## <span id="page-15-3"></span>4.3 Trouble is...

## 4.3.1 Installing

Here is the story why you get error messages installing PARRATT32: Since Inprise (formerly known as Borland) changed their database engine (BDE) to version 5.0 and gave it away for free, I thought it might be a good idea to have it on my system. It also had the advantage of being the english language version which was not available to me in version 4.52. But, the



Installshield Express Delphi Edition that came with Delphi 3.0 (which was the development tool for PARRATT32) was not working correctly any more with this edition of the BDE. The support site of 'Installshield.com' had a little work–around for about two weeks in the late summer of 1998. It didn't work error free (as you see) but at least is does not prevent the installation of the software, completely. Then they stopped supporting this version of their software and removed the patch from their server. In the meanwhile Inprise came out with Delphi 4 which was bundled with a) the BDE 5.0 and b) a new version of Installshield Express Delphi Edition. But this also means that people like me, who do not own a Delphi 4 or an InstallShieldExpress 2.03 will never be able to make correctly working sets of installation media.

All this only concerns the installation of PARRATT32. Once installed there are no known problems with BDE 5.0!

## 4.3.2 The Decimal Separator

What is a decimal separator most people will ask, especially when they are from english speaking countries. However, in Germany for instance the decimals of a real number are separated from the integer part by a comma. Microsoft Windows handles this with a setting in the control panel ("International" or "Systemsteuerung–Ländereinstellungen" in the german version). When you have installed PARRATT32 and switch the decimal separator setting later on in either direction you will get some error messages concerning not–valid–floating–point– values: don't be surprised. PARRATT32 tries to translate all these numbers depending on the settings you chose on your system with these exceptions: a) Values that were stored in the edit fields of some of the dialogue boxes (i.e. the 'settings' or the 'FitIt' dialogue) cannot be converted on-the-fly since you typed them in! when PARRATT32 complains about these values try to look them up and correct them manually. b) Values are stored in the Windows' registry according to the current decimal separator setting, so after changing the separator setting while PARRATT32 is not running these values are not longer valid and the programme will load default values instead of the ones found in the registry.

Always remember what decimal separator setting you have on your system and type in numbers according to this setting. PARRATT32 is no wizard knowing that you meant "1.541" but Windows said you should have typed "1,541"!

# <span id="page-17-0"></span>5 The Source Code

PARRATT32's language is Pascal. Since Pascal on a PC means Borland Turbo Pascal and programming graphical user interfaces for PCs means Microsoft Windows the right tool is called Delphi. Borland stopped calling its Pascal compiler Pascal after Borland Pascal 7.0, then came Delphi 1 (BP 8.0), Delphi 2 (BP 9.0) and Delphi 3. The command-line compiler says Delphi for Win32 version 10.0...

You do not have to know anything about Windows programming to understand the source code of PARRATT32 and the use of Delphi — there is nothing like int APIENTRY WinMain(hinstance, hinstPrev, lpCmdLine, nCmdShow) like in C++ — , but a little knowledge of Pascal is recommended.

## <span id="page-17-1"></span>5.1 The Code Itself

## 5.1.1 Naming conventions

I tried to keep a reasonable naming scheme for the objects in the programme, variables, functions and procedures as well as for classes. The visual components all have a prefix to determine of what type they are:



## 5.1.2 Globals

This is the file called globals, pas where all the global constants, types and variables are stored. It's not too much I guess...

```
1 unit Globals;
2 {************************************************************************}
 3 { some constants and some types that are used globally }
4 {************************************************************************}
5 interface
6
        const { some upper array boundaries and misc. constants }
8 maxLayers = 499;<br>9 maxMalues = 999;
9 maxQValues = 999<br>10 map = maxLayers*
10 map = maxLayers*4+10;<br>11 { different values for<br>12 simplesample = 1;
                 11 { different values for variable 'sampletype' }
 12 simplesample = 1;
13 functionsample = 2;
14 multisample = 3;
 15 { different function types }
16 ft_builtin = 0;
17<br>
16 ft_builtin =<br>
17 ft_user = 1;<br>
18 f Window IDs}<br>
19 wnd_Plot = 1
                 18 { Window IDs}
19 wnd_Plot = 1;<br>20 wnd_Model = 2<br>21 wnd Profile =
                    wnd\_Model = 2;21 wnd_Profile = 3;<br>
22 { dataset IDs}<br>
23 ds_data = 0;<br>
ds_calc = 1;<br>
25 ds_prof = 0;
                {4} dataset IDs}23 ds_data = 0;
24 ds_calc = 1;
25 ds_prof = 0;<br>
26 ds_minus = 2<br>
27 ds plus = 3;
 26 ds_minus = 2;
27 ds_plus = 3;
28 ds_trans = 4;
```

```
\begin{tabular}{ll} 29 & & ds\_fitwindow = 9; \\ 30 & { Help IDs} \\ 31 & & hclndex = 10; \end{tabular}30 { Help IDs}
31 hcIndex = 10;
32 hcfrmPlot = 80;
33 hcfrmModel = 40;
34 hcfrmProfile = 70<br>35 fittingdialog = 39
35 fittingdialog = 350;<br>36 fittingdialog = 350;<br>37 functiondialog = 340
36 settingsdialog = 330;
37 functiondialog = 340;
38 DatabaseEditor = 375;
\frac{39}{40}RegFilename = '\SOFTWARE\HMI\Parratt32';
\frac{41}{42}42 type float = double;<br>43 flarray = array43 flarray = array[-5. maxLayers*4+5] of float;<br>44 Pflarray = ^flarray;
44 Pflarray = ^flarray;
45 flarray1 = array[0..maxQValues] of float;
46 PFlarray1 = ^flarray1;
47 IntegerArrayMFIT = ARRAY [1..map] OF integer;
47 Fitariayi - Isairayi, 1888<br>48 FitParameter = array[1..maxLayers*4+10] of float;
\frac{49}{50}50 var a: Pflarray; { layer parameters for fitting }
51 q, refl, errors: Pflarray1; { loaded data }
52 resltn, bg: Pflarray1; { resolution and background }
53 ndata: integer; financy, interviewed and a magnetic state of datapoints in loaded data<br>54 nlparms: integer; finance of layer parameters<br>55 c_MinZ, c_MaxZ: integer; finance of layer parameters<br>56 dataavail, hasbeenfitted
                                                                               f number of layer parameters
                 nlparms: integer;<br>c_MinZ, c_MaxZ: integer;
56 dataavail, hasbeenfitted, expert,<br>57 splashing, databaseing: Boolean;<br>58 sampletype, functiontype: Byte;
57 splashing, databaseing: Boolean;
58 sampletype, functiontype: Byte;
59 fitwindow: array[0..1] of float;<br>60 www_hmi, www_bensc, author_e_mai
                  www_hmi, www_bensc, author_e_mail: String;
                 datafilename, fn_databasename: String;
61<br>62implementation
63<br>64<br>6565 {************************************************************************}
66
\frac{67}{68}68 end.
```
#### 5.1.3 Fequently Used Functions And Procedures

The file rtfuncs.pas contains most of the frequently used things, which are not directly related to events produced by the user interface, such as mouse clicks or menu messages. The following code shows the definition or interface part of this file

```
1 unit RTFuncs;<br>2 f here are so
2 { here are some functions that are used by all modules }
3 interface
4
5 uses Forms, Windows, SysUtils, Controls, Graphics, Dialogs, Printers, Classes,
               Menus, db, dbtables, xyGraph,
               numus, un<br>Globals;
8
      procedure LoadReflData;
10 procedure SaveReflData;<br>11 procedure LoadModelData
11 procedure LoadModelData;<br>12 procedure SaveModelData;
12 procedure SaveModelData;<br>13 procedure SaveProfileDat
13 procedure SaveProfileData;<br>14 procedure SaveUserFunction
14 procedure SaveUserFunction;<br>15 procedure LoadUserFunction;
15 procedure LoadUserFunction;<br>16 procedure LoadDatabase:
16 procedure LoadDatabase;<br>17 procedure PletData:
17 procedure PlotData;<br>18 procedure PrintResu
18 procedure PrintResults;
19 function EvalFunc(z, rhostart, rhoend, p_A, p_B, p_C, p_D, p_E: double): double;
20 procedure GetParameters(magnsign: Integer);<br>21 procedure PutParameters;
      procedure PutParameters;
\frac{22}{23}implementation
24 .
25 .
\frac{20}{26}27 end.
```
In brief these functions and procedures perform the following tasks:

<span id="page-19-0"></span>

#### 5.1.4 The Calculation of the Reflectivity

The Parratt formalism is coded in the file uparratt.pas according to the following formula:

wave vector inside layer *n*: 
$$
k_{z,n} = \sqrt{k_{z,0}^2 - 4\pi\rho_n}
$$
  
reflectivity from layer *n*: 
$$
r_{n,n+1} = \frac{k_{z,n} - k_{z,n+1}}{k_{z,n} + k_{z,n+1}} \cdot e^{-2\sigma_{n+1}^2 k_{z,n} k_{z,n+1}}
$$
  
reflectivity of the system: 
$$
R = |R_0|^2
$$

$$
R_{N+1} = 0
$$

$$
R_N = r_{N,N+1}
$$

$$
R_n = \frac{r_{n,n+1} + R_{n+1}e^{2id_{n+1}k_{z,n+1}}}{1 + r_{n,n+1}R_{n+1}e^{2id_{n+1}k_{z,n+1}}}
$$

NB:  $\rho_n$  is complex:  $\rho_n = \rho_n + i\text{Im}(\rho_n)$ , where  $\rho_n$  and  $\text{Im}(\rho_n)$  are the values given in the model window.

The source is somewhat documented. Only a few remarks: procedures kadd, ksub, kmul, kdiv, kexp, and ksqrt all work on complex numbers (type kompl) and are defined in cxmath.pas. Since Pascal knowns no way of passing back user defined types in functions these all had to be made procedures that pass back the result in the last argument. For this reason there is heavy use of temporary variables in the code. The *bare* reflectivity is calculated by  $c$ Parratt $(\ldots)$ , whereas the plotting routine calls CalcParratt(...), where things like background and resolution are handled.

```
1 unit Uparratt;
2 {************************************************************************}
3 { This Unit calculates the reflectivity of a n-layer system at given Qz }
4 { R(Qz) := cParratt(Qz, resolution, nlayers, parameters) }
5 { }
\begin{array}{ccc} 6 & \{ \end{array}
```
#### 5.1 THE CODE ITSELF



```
7 { input is as follows: }<br>8 { double Qauble Qz: z-component of the scattering vector } }<br>9 { double Resolution: Qz-resolution
10 { double Resolution: Qz-resolution<br>10 { integer nlayers: number of layers (no bulk, no vacuum)<br>11 { pointer parameters: points to an array of the following p
11 { pointer parameters: points to an array of the following parameters:<br>12 { narameters ii = rho(air)
12 { parameters[1] := rho(air) }<br>13 { [2] := Imrho(air) }
14 { [3] := d(1st layer) }<br>15 { [4] := rho(1st layer) }<br>16 { [5] := Imrho(1st layer) }
17 { [6] := sigma(1st layer)<br>18 {
18 { ... }
19 { [4*nlayer+3] := d(nth layer) }
20 { \{ [4*nlayer+6] := sigma(nth layer) }<br>22 { \{ [4*nlayer+7] := rho(bulk) }<br>23 { \{ [4*nlayer+8] := Imrho(bulk) }
24 { [4*nlayer+9] := sigma(bulk) }
25 \t {example:}<br>26 \t {for a si}}
26 { for a single interface there will be 5 parameters:<br>27 { rho(air), Imrho(air), rho(bulk), Imrho(bu
                        27 { rho(air), Imrho(air), rho(bulk), Imrho(bulk), sigma(bulk) }
\begin{array}{c} 28 \\ 29 \\ 30 \end{array}{
29 { d is in Angstroms (AA) }
30 { rho is in AA^-2: rho_el * r_0 for x-rays, }
                                                                                                                        }
31 { Nb for neutrons }
32 { Imrho is in AA^-2: calculated from beta for xrays, }
33 { calculated from abs. cross section for neutrons }
34 { sigma is in AA }
35 {************************************************************************}
\frac{35}{36}interface
\frac{37}{38}uses Globals, cxmath;
\frac{40}{41}41 function calcParratt(qz, rsltn, bg: float;
42 nlayers: integer; parameters: Pflarray;
43 UseRsltn, UseBG: Boolean): float;
\frac{44}{45}implementation
\frac{46}{47}var rrn: array[0..maxLayers+1] of kompl;
\frac{48}{49}49 function cParratt(qz: float; nlayers: integer; parameters: Pflarray): float;
\begin{array}{cc} 50 & \text{var} \\ 51 & \\ 52 & \end{array}51 d, rho, imrho, sigma: array[0..maxLayers] of float;
52 rcc, rnn1, arg, temp1, temp2, num, den: kompl;
53 n : integer;
54 e2idk, rme: kompl;<br>55 kz0: float;
             kz0: float:
\frac{56}{57}<br>\frac{58}{59}57 procedure kzn(kz0: float; ni: integer; var res: kompl);
            prossaars nan(nis<br>var radix: kompl;
59 begin
60 radix[1] := kz0*kz0-4*pi*rho[ni];
61 radix[2] := 4*pi*imrho[ni]; // changed 08-02-98, cb
62 ksqrt(radix, res);
62 ks<br>63 end:
64<br>6565 procedure rn(kz0: float; ni: integer; var res: kompl);
66 var kz_n, kz_np1, rnum, rden, e2kks, rfres, arg1, arg2: kompl;
67 begin<br>
68 kzn(<br>
69 kzn(
68 kzn(kz0, ni, kz_n);
69 kzn(kz0, ni+1, kz_np1);
70 ksub(kz_n, kz_np1, rnum);
71 kadd(kz_n, kz_np1, rden);
72 kdiv(rnum, rden, rfres);
73 { include roughness according to Nevot & Croce }
74 kmul(kz_n, kz_np1, arg1);
75 rmul(-2*sqr(sigma[ni+1]), arg1, arg2);
76 kexp(arg2, e2kks);
77 kmul(rfres, e2kks, res);
          end:
^{77}_{77}<br>^{78}_{79}<br>^{80}_{80}80 begin
81 { map parameters^[] to d[], rho[], my[], sigma[] }<br>82 rho[0]:= parameters^[1];<br>83 imrho[0]:= parameters^[2];
84 { calculate wavevector kz0': 1. vacuum, air -> Qz/2 }
85 { 2. n0 <> 0 -> sqrt(Qz0^2/4+4*pi*rho0+4*pi*mu0)}
86 temp1[1] := qz*qz/4+4*pi*rho[0];<br>87 temp1[2] := 4*pi*imrho[0];
87 temp1[2] := 4*pi*imrho[0];<br>88 ksart(temp1.temp2):
88 ksqrt(temp1, temp2);
89 kz0 := kabs(temp2);
```
90 for n := 1 to nlayers do



```
\begin{tabular}{ll} 91 & &begin{array}{l} &begin{array}{l} \\ \end{array} \end{tabular} \end{tabular} \begin{tabular}{ll} 91 & &begin{array}{l} \\ \end{array} \end{tabular} \end{tabular} \begin{tabular}{ll} 93 & & \end{tabular} \end{tabular}92 d[n] := abs(parameters^[(n-1)*4+3]); // abs() added 22-01-98<br>93 rho[n] := parameters^[(n-1)*4+4];<br>94 imrho[n] := parameters^[(n-1)*4+5];<br>95 sigma[n] := parameters^[(n-1)*4+6];
96 end;<br>97 rho[nl
97 rho[nlayers+1] := parameters^[nlayers*4+3];<br>98 imrho[nlayers+1] := parameters^[nlayers*4+4
98 imrho[nlayers+1] := parameters^[nlayers*4+4];
99 sigma[nlayers+1] := parameters^[nlayers*4+5];
100 { done with remapping }<br>101 rrn[nlayers+1, 1] := 0;<br>102 rrn[nlayers+1, 2] := 0;<br>103 { calculate rrn[nlayers]: bulk interface }
104 rn(kz0, nlayers, rrn[nlayers]);
105 { calculate the rrn[...] for the remaining layers }
\begin{array}{lll} 106 & \text{ for n} := \texttt{nlayers-1} \texttt{ downto 0 do} \\ 107 & \texttt{begin} \end{array}\frac{107}{108} begin<br>\frac{108}{108}108 rn(kz0, n, rnn1); { r_n,n+1 }<br>
109 kzn(kz0, n+1, temp1); { k_z,n+1 }<br>
110 arg[1] := 2*d[n+1]; <br>
111 arg[2] := 2*d[n+1];
112 kmul(temp1, arg, temp2); { 2 * i * k_z,n+1 * z_n+1 }
113 kexp(temp2, e2idk);
114 kmul(e2idk, rrn[n+1], rme); { X_n+1 * exp(2 i k_z,n+1 z_n+1) }
115 kadd(rnn1, rme, num); { r_m,n+1 + X_n+1 * exp(---) }<br>116 kmul(rnn1, rme, den); { r_m,n+1 * X_n+1 * exp(---) }
mattezia, \lim_{t \to 1}, \lim_{t \to 0}<br>
115 kadd(rnn1, rme, num);<br>
117 den[1] := den[1] + 1;<br>
118 kdiv(num, den, rrn[n])
118 kdiv(num, den, rrn[n]);<br>119 end:119 end;
120 rcc[1] := rrn[0,1]; rcc[2] := -1*rrn[0,2];
121 kmul(rrn[0], rcc, temp1);
122 cParratt := temp1[1];
123 end;
\frac{120}{124}125 function calcParratt(qz, rsltn, bg: float;
126 nlayers: integer; parameters: Pflarray;
127 Usersltn, UseBG: Boolean): float;
128 var refl: float;
129 begin
130 refl := cParratt(qz, nlayers, parameters);
131 if UseRsltn then
132 begin<br>133 far
133 { approximate Gaussian beam profile by 8 pivot points }<br>134 refl := refl + 0.135*cParratt(qz-rsltn, nlayers, parame
134 refl := refl + 0.135*cParratt(qz-rsltn, nlayers, parameters);<br>135 refl := refl + 0.135*cParratt(qz+rsltn, nlayers, parameters);<br>136 refl := refl + 0.325*cParratt(qz-rsltn*3/4, nlayers, parameters);<br>137 refl := refl + 0
138 refl := refl + 0.605*cParratt(qz-rsltn/2, nlayers, parameters);<br>139 refl := refl + 0.605*cParratt(qz+rsltn/2, nlayers, parameters);
139 refl := refl + 0.605*cParratt(qz+rsltn/2, nlayers, parameters);
140 refl := refl + 0.88*cParratt(qz-rsltn/4, nlayers, parameters);
141 refl := refl + 0.88*CParent(qz+rsltn/4, nlayers, parameters);<br>142 refl := refl/4.89;142 refl := refl/4.89;<br>143 end:
143 end;<br>144 if UseE
144 if UseBG then refl := refl + bg;<br>145 calcParratt := refl:
             calCalcParratt := refl:
146 end;<br>147 end.
         end.
```
#### 5.1.5 The Calculation of the Transmission

Calculation of the transmission of "free samples" is done according to the following formula:

$$
T(Q_z) = (1 - R(Q_z))T_{\text{subst}}(Q_z)
$$

where  $T_{\text{subst}}(Q_z)$  is the transmission through the substrate, which is calculated by the following code:

```
1 function calcTrans(qz: float; nlayers: integer; parameters: Pflarray;<br>2 wavelength, substratethickness: float): float:
2 wavelength, substratethickness: float): float;
3 var pathlength: float;<br>4 d. rho. imrho: float
4 d, rho, imrho: float;
5 temp1, temp2, temp3: kompl;
6 n: integer;
            currentk: kompl;
8 \tbegin{array}{c} 8 \\ 9 \end{array} begin
9 pathlength := 0;
10 for n := 1 to nlayers do
11 begin
```
<span id="page-22-0"></span>

#### 5.1.6 Calculation of the Scattering Length Density Profile

The calculation of the scattering length density profile from the given layers in the model is done by evaluating the following formula:

$$
\varrho(z) = \sum_{i=1}^{N} \frac{\varrho_i - \varrho_{i+1}}{2} \left( 1 + \text{erf}\left(\frac{z - z_i}{\sqrt{2}\sigma_i}\right) \right),
$$

where N is the overall number of layers,  $\rho_i$  is the scattering length density of the *i*th layer at position  $z_i$  and with a gaussian roughness  $\sigma_i$ . The error function erf(x) is approximated by a 5th order polynomial given by Press et al.[\[Press88\]](#page-27-3).

```
1 procedure TfrmProfile.ShowProfile;<br>2 var i. i. s index. r index. d inde
2 var i, j, s_index, r_index, d_index,
3 lastlayer, zstart, zend, temp: integer;
\frac{1}{4} z, zinc, sum,
                  deltarho, sigma, zi: float;
\begin{array}{c} 5 \\ 6 \\ 7 \end{array}function erfcc(x: float): float; { according to 'NumRecip' }
\begin{matrix} 8 & 7x \\ 9 & 1 \end{matrix}9 t,z,ans: extended;<br>10 begin
\begin{tabular}{ll} 10 & begin \\ 11 & z : \\ 12 & t : \end{tabular}z := abs(x);12 t := 1.0/(1.0+0.5*z);<br>13 trv13 try
14 ans := t*exp(-z*z-1.26551223+t*(1.00002368+t*(0.37409196+t*(0.09678418
15 +t*(-0.18628806+t*(0.27886807+t*(-1.13520398+t*(1.48851587
15 \begin{aligned} \text{16} & +1 \times (-0.18628806 + t*(0.27886807 + t*(-1.13\\ + t*(-0.82215223 + t*0.17087277)))))\text{)}\text{17} \\ \text{18} & +t*(-0.82215223 + t*0.17087277)))))\text{)}\text{18} \end{aligned}\begin{tabular}{cc} 17 & & \texttt{except} \\ 18 & & \texttt{ans} \\ 19 & & \texttt{end} \end{tabular}ans := 0;
\begin{tabular}{ll} 19 & \quad \quad \mathsf{end}; \\ 20 & \quad \quad \mathsf{if} \ \ \mathtt{x} \end{tabular}20 if x > = 0.0 then erfcc := ans<br>21 else erfcc := 2.0-ans
21 else erfcc := 2.0-ans<br>22 end;
              end;
\begin{array}{c} 23 \\ 24 \\ 25 \end{array}begin
25 Screen.Cursor := crHourGlass;<br>26 GetParameters(0);<br>27 xvGraph1[ds prof].Free:
26 GetParameters(0);
27 xyGraph1[ds_prof].Free;
28 xyGraph1.Plotting := False;<br>28 xyGraph1.Plotting := False;
\begin{tabular}{ll} 29 & \hspace{15pt}\text{with xyGraph1[ds\_prof] do} \\ 30 & \hspace{15pt}\text{begin} \end{tabular}30 begin<br>31 Draw
31 DrawPoints := False;<br>32 LineColor := clBlack<br>33 end;
                      LineColor := c1Black;33 end;<br>34 if Set<br>35 with
              if SettingsDlg.cbUserZ.Checked then
35 with SettingsDlg do<br>36 begin<br>37 zstart := edtMi
                      begin
                          -<br>zstart := edtMinZ.Value;
```

```
38 zend := edtMaxZ.Value;<br>39 if zstart > zend then<br>40 begin
                     if zstart > zend then
40 begin<br>41 town
41 temp := zstart;<br>42 zstart := zend;
42 zstart := zend;<br>43 zend := temp;<br>44 end;
                            zend := temp;end;\frac{45}{46}46 else CalcZBounds(zstart, zend);<br>47 z := zstart:
47 z := zstart;<br>48 zinc := (zene
48 zinc := (zend-zstart)/SettingsDlg.edtNumPointsZ.Value;<br>
49 while z <= zend do<br>
50 begin<br>
51 lastlayer := 0;
           while z \le zend do
              50 begin
51 lastlayer := 0;<br>52 case sampletype<br>55 simplesample:<br>55 lunctionsample:<br>55 lunctionsampl<br>56 lastlayer :<br>57 multisample:<br>58 lastlayer :
                  case sampletype of
                    simplesample:
                        lastlayer := frmModel.edtLayers.Value;
55 functionsample:
56 lastlayer := frmModel.edtLayers.Value+frmModel.edtNumCalcLayers.Value;
                    multisample:
                       58 lastlayer := frmModel.edtLayers.Value
59 +frmModel.edtRepts.Value*frmModel.edtStackedLayers.Value;<br>60 end;<br>61 sum := a^[1];
60 end;
61 sum := a^[1];
62 sum : - a ti,<br>
62 for i:= 1 to lastlayer+1 do<br>
63 begin<br>
65 begin
                  begin
                     if i = lastlayer+1 then65 begin
66 r_index := 4*i-1; { rho_bulk }
67 s_index := r_index+2; { sigma_bulk }
68 if last<br>layer = 0<br>69 then deltarho:
69 then deltarho := a^[r_index] - a^[r_index-2]<br>70 else deltarho := a^[r_index] - a^[r_index-3];
70 else<br>
71 end else<br>
72 end else<br>
8 end else<br>
73 sinner<br>
75 fi i the political end;<br>
77 else<br>
80 i := 1;<br>
80 i := 1;
72 begin
73 s_index := 4*i+2;
74 r_index := 4*i;
75 if i = 1
76 then deltarho := a^[r_index]-a^[r_index-3]<br>77 else deltarho := a^[r_index]-a^[r_index-4];
                            end;
79 zi := 0;
80 j := 1;
81 \begin{array}{ccc} 3 & 1 & 1 \\ 81 & 1 & 1 \end{array} then while jsi do<br>82 begin<br>83 d_index := 4*(j-1)+3<br>84 zi := zi + a^[d_index
82 begin<br>
83 d_index := 4*(j-1)+3;<br>
84 zi := zi + a^[d_index];
85<br>
86<br>
87<br>
11 := 2<br>
11 = 2<br>
100(j);<br>
116 (j);<br>
15 (s)end:
87 i \text{ a}^{-1}\text{ s}_2 \text{ index} = 0 then sigma := 1e-3<br>88 else sigma := \text{a}^{-1}\text{ s}_2 \text{ index};<br>89 sum := sum + deltarho/2*(2-erfcc((z-z<br>90 end;
88 else sigma := a^[s_index];
89 sum := sum + deltarho/2*(2-erfcc((z-zi)*sqrt(2)/2/sigma)); // changed on 24-NOV-99
90 end;<br>91 xyGraph<br>92 Form1.9
                  91 xyGraph1[ds_prof][z] := sum;
92 Form1.Statusbar1.Panels[0].Text :=<br>93 Format('calculating rho(z), z<br>94 Form1.Statusbar1.Refresh:
                        Format('calculating rho(z), z = \frac{9}{1}; [z]);
94 Form1.Statusbar1.Refresh;<br>95 z := z + zinc;<br>96 end;
                  z := z + zinc;96 end;<br>97 Screen
97 Screen.Cursor := crDefault;<br>98 xvGraph1.Dimensions.YAxisTi
98 xyGraph1.Dimensions.YAxisTitleOffset := 20;<br>99 xyGraph1.Plotting := True;<br>100 Form1.Statusbar1.Panels[0].Text := '';
99 xyGraph1.Plotting := True;
100 Form1.Statusbar1.Panels[0].Text := '';
101 end;
```
#### 5.1.7 Fitting of A Model to Reflectivity Data

The code for the optimization of the layers's parameters is a little too complex to be described in just one formula. The minimization is done by least squares fitting:

$$
\chi^2 = \sum_{i=1}^M \left( \frac{R^{\rm calc}_{Q_{z,i}} - R^{\rm meas}_{Q_{z,i}}}{\rm weighting} \right)^2,
$$

where weighting is either 1 ("no weighting") or  $R_{Q_{z,i}}^{\text{meas}}$  ("statistical weighting") or  $\delta R_{Q_{z,i}}^{\text{meas}}$  ("error weighting"), see function  $\texttt{CalcChisq(weight: integer)}$  for details, and M is the num-

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ber of datapoints. The parameter minimization is done in the procedure Newton(parindex: integer), which is a simple Newton method for finding minima in parametric functions. It in(de)creases the parameter value until the difference in  $\chi^2$  between two successive steps falls below a given threshold (edtTolerance.Value). The rest of the code deals with chosing of parameters, fitting regions in  $Q_z$  etc.

```
1 procedure TFitDlg.btn1iterClick(Sender: TObject);<br>2 uar i i puarpar PB: integer:
        2 var i, j, nvarpar, RB: integer;
3 lista, listadone: IntegerArrayMFIT;<br>
4 chise chiold chidiff: real:
4 chisq, chiold, chidiff: real;
5 finished: Boolean;
6 iter: longint;
7 nol, weightingmethod : integer;<br>8 lastvarpar: integer;<br>9 FitndataStart, FitndataEnd: int.
8 lastvarpar: integer;
9 FitndataStart, FitndataEnd: integer;
\begin{array}{c} 10 \\ 11 \\ 12 \end{array}function CalcChisq(weight: integer): float;
12 var cref, cs: float;<br>13 i: integer;
13 i: integer;<br>
14 begin<br>
15 cs := 0;
14 begin
15 cs := 0;
16 if cbDisplayGraph.Checked then<br>17 begin<br>18 frmPlot.xyGraph1.Plotting<br>19 frmPlot.xyGraph1[ds_calc].1
                 begin
18 frmPlot.xyGraph1.Plotting := False;
19 frmPlot.xyGraph1[ds_calc].Free;
20 with frmPlot.xyGraph1[ds_calc] do<br>21 begin<br>22 DrawPoints := false;
                       begin
22 DrawPoints := false;<br>23 LineColor := clBlack<br>24 end;
                           LineColor := c1Black;\begin{tabular}{ll} 24 & & \textbf{end;} \\ 25 & & \textbf{end;} \end{tabular}\begin{array}{cc} 25 & \text{end}; \\ 26 & \text{for } i \end{array}26 for i:= fitndataStart to fitndataEnd do<br>27 begin<br>28 cref := calcParratt(q^[i], resltn^[i]
                 begin
28 cref := calcParratt(q^[i], resltn^[i], bg^[i],<br>29 nol, a, cbRsltn.Checked, cl
29 case weight of \begin{bmatrix} 29 & 213 \\ 20 & 212 \end{bmatrix} case weight of
30 case weight of<br>31 1: cs := cs ·<br>32 2: cs := cs ·
31 1: cs := cs + sqr((refl^[i]-cref)/errors^[i]);<br>32 2: cs := cs + sqr((refl^[i]-cref)/refl^[i]);
33 3: cs := cs + sqr(ref1^{r}[i]-cref);<br>34 end;
\begin{tabular}{ll} 34 & \hspace{1.5mm} end; \\ 35 & \hspace{1.5mm} if c \\ 36 & \hspace{1.5mm} end; \end{tabular}35 if cbDisplayGraph.Checked then frmPlot.xyGraph1[ds_calc][q^[i]] := cref;
36 end;<br>37 CalcCh<br>38 if cbD
              \text{CalcChisq} := \text{cs/}( \text{fithdataEnd-fithdataStart});
38 if cbDisplayGraph.Checked then<br>39 begin<br>40 frmPlot.xyGraph1.Plotting
39 begin
40 frmPlot.xyGraph1.Plotting := True;
11 1blChisq.Caption := FormatFloat('0.0000E+00',<br>42 cs/(fitndatal
                                                                       42 cs/(fitndataEnd-fitndataStart));
                 end;
           end:
43<br>44<br>45<br>4646 procedure Newton(parindex: integer);<br>47 var incr, fac, newchisq: float;<br>48 begin
            .<br>var incr, fac, newchisq: float;
48 begin<br>49 chis<br>50 if I<br>51 fac<br>52 item
49 chisq := CalcChisq(weightingmethod);
50 if P[parindex]=0 then incr := 1e-7 else incr := P[parindex] * 0.1;
51 fac := 1;
52 iter := 0;
53 repeat<br>54 repeat<br>55 in
                 repeat
55 inc(iter);<br>56 Form1.Stat<br>57 Form1.Stat<br>59 P[parindex
                    56 Form1.StatusBar1.Panels[0].Text := IntToStr(parindex)+' : '
                                                                           57 +IntToStr(iter);
                    Form1.Statusbar1.Refresh;
59 P[parindex] := P[parindex]+incr*fac;<br>60 CalcAfromP;<br>61 if cbDisplayGraph.Checked then ListB
                    CalcAfromP;
61 if cbDisplayGraph.Checked then ListBoxUpdate;<br>62 newchisq := CalcChisq(weightingmethod);
62 newchisq := CalcChisq(weightingmethod);
63 chidiff := chisq-newchisq;
64 if chidiff <0 then<br>65 begin
65 begin<br>66 fac<br>67 P[pa
66 fac := -fac;
67 P[parindex] := P[parindex]+incr*fac;
68 end else<br>69 begin
69 begin<br>70 chi:<br>71 fac
70 chisq := newchisq;
71 fac := fac*2;
72 end;
73 Application.ProcessMessages;
ry<br>
T2 and;<br>
T3 Application.ProcessMessages;<br>
T4 until (chidiff<0) or (iter>99);
```
#### 5.1 THE CODE ITSELF



```
75 fac := fac/2;<br>76 Application.F<br>77 if ModalResul<br>78 until ((abs(chi
76 Application.Processmessages;
77 if ModalResult = mrCancel then stopfitting := True;
78 until ((abs(chidiff)<=edtTolerance.Value) and (iter>2)) or stopfitting;
79 end;
\begin{array}{c} 80 \\ 81 \end{array}\begin{tabular}{ll} 81 & begin \\ 82 & sto \\ 83 & con \end{tabular}82 stopfitting := False;
83 converged := False;
84 lblconverged.Visible := False;
85 btnStop.Enabled := True;<br>86 Screen.Cursor := crHourG
86 Screen.Cursor := crHourGlass;
87 { set weighting method }
88 if RBNone.Checked then weightingmethod := 3;<br>89 if RBStat.Checked then weightingmethod := 2;
89 if RBStat.Checked then weightingmethod := 2;<br>90 if RBErrors.Checked then weightingmethod := 2;
90 if RBErrors.Checked then weightingmethod := 1;
91 { get variable parameters from CheckListBox1 }
92 nvarpar := 0;
93 i := 0;
94 while i <= CheckListBox1.Items.Count-1 do
95 begin<br>96 begin<br>96 if 0
96 if CheckListBox1.Checked[i] then<br>97 begin<br>98 lista[nvarpar+1] := i+1:
97 begin
98 lista[nvarpar+1] := i+1;
99 inc(nvarpar);<br>100 end;
100 end;<br>101 inc(i)
101 inc(i);<br>102 end:
\begin{tabular}{ll} 102 & end; \\ 103 & { set } c \\ 104 & no1 := \end{tabular}103 { set overall number of layers }
104 nol := frmModel.edtLayers.Value;
105 case sampletype of<br>106 functionsample: n
106 functionsample: nol := nol + frmModel.edtNumCalcLayers.Value;
107 multisample: nol := nol + frmModel.edtStackedLayers.Value
108 *frmModel.edtRepts.Value;
\begin{array}{cc} 109 & \text{end} \\ 110 & \{ \text{ge} \} \end{array}110 { get fitting region }
111 if (fitwindow[0] = -1) and (fitwindow[1]=-1) then
112 begin { no user region specified }
113 fitndataStart := 1;
114 fitndataEnd := ndata;
115 end else<br>116 begin
116 begin { user has specified a region }<br>117 i := 0116 begin<br>
117 i := 0;<br>
118 repeat
118 repeat<br>119 inclusion
119 inc(i);<br>120 until (i > ndata) or (q^[i] > fitwindow[0]);
121 fitndataStart := i-1;<br>122 i := 0;
122 i := 0;<br>123 repeat
123 repeat
124 inc(i);
125 until (i > ndata) or (q^[i] > fitwindow[1]);<br>126 fitndataEnd := i-1;
\begin{tabular}{cc} 127 & end; \\ 128 & \{ check \end{tabular}128 { check if user wants to fit or only the chisq }<br>129 RB := 0:
129 RB := 0;<br>130 if RBchi
130 if RBchisq.Checked then RB := 1;<br>131 if RBfulliter.Checked then RB :=
131 if RBfulliter.Checked then RB := 2;<br>132 case RB of
           case RB of
133 1: blchisq.Caption := FormatFloat('0.0000E+00', CalcChisq(weightingmethod));<br>134 2: begin
134 2: begin<br>135 \{ \cdot \}135 { 'make' all parameters are still unminimized }<br>136 for i := 1 to nvarpar do listadone[i] := 1;<br>137 finished := False;
138 lastvarpar := -1;
139 repeat<br>140 if n
140 if nvarpar > 1 then<br>141 repeat
141 repeat<br>142 i =
142 j := Trunc(Random*nvarpar)+1;<br>
143 until j <> lastvarpar<br>
144 else j := 1;<br>
145 lastvarpar := j;<br>
146 if listadone[j]=1 then
147 begin<br>148 chi
148 chiold := CalcChisq(weightingmethod);<br>149 Newton(lista[j]);
149 Newton(lista[j]);
150 if chisq<chiold then for i:=1 to nvarpar do listadone[i]:=1
11 chief chief and the first interest of 1.1 to health<br>
151 else listadone[j] := 0;<br>
152 end.
152 end;<br>153 1b1Chi
153 lblChisq.Caption := FormatFloat('0.0000E+00', chisq);<br>154 f replot the graph }
154 { replot the graph }
155 frmPlot.xyGraph1.Plotting := False;
156 frmPlot.xyGraph1[ds_calc].Free;
157 with frmPlot.xyGraph1[ds_calc] do
158 begin
```


```
159 DrawPoints := false;<br>160 \text{LineColor} := clBlack
160 LineColor := clBlack;<br>161 end;
161 end;<br>162 for i.
162 for i := fitndataStart to FitndataEnd do<br>163 frmPlot.xyGraph1[ds_calc][q^[i]] :=
163 frmPlot.xyGraph1[ds_calc][q^[i]] :=<br>164 calcParratt(g^[i] resltn^[i] h
164 calcParratt(q^[i], resltn^[i], bg^[i], nol, a,<br>165 conducts result the checked, cbBackground.Checked);
166 frmPlot.xyGraph1.Plotting := True;
167 { update the parameters in CheckListBox1 }
168 ListBoxUpdate;<br>169 { check for 'u
169 {169} {169} {170} {1, 50} {1, 60} {1, 10} {1, 10} {1, 10} {1, 10} {1, 10}170 j := 0;<br>
171 for i:= 1 to nvarpar do j:= j+listadone[i];<br>
172 if j=0 then converged := True;<br>
173 if (ModalResult = mrCancel) or stopfitting then finished := True;<br>
174 until (chisq<edtTolerance.Value) or finished or c
175 if converged then lblConverged.Visible := True;<br>176 CalcAfromP:
176 CalcAfromP;<br>177 Form1.Statu
177 Form1.StatusBar1.Panels[0].Text := '';<br>178 end:
          end;<br>end;
\frac{179}{180}180 btnStop.Enabled := False;<br>181 Screen.Cursor := crDefaul
181 Screen.Cursor := crDefault;
182 MessageBeep(0);
183 Application.ProcessMessages;
184 end;
185
```
## <span id="page-26-0"></span>5.2 Compiling

#### 5.2.1 What you need...

- 1. The sources. These can be obtained from Christian Braun by e–mail: [braun@atmos.umnw.ethz.ch](mailto:braun@atmos.umnw.ethz.ch) or ask Roland Steitz [\(steitz@hmi.de\)](mailto:steitz@hmi.de) for my whereabouts.
- 2. A complete installation of Delphi. Version 3 professional is recommended, version 2 could work, version 4 does work.
- 3. The following non–standard Delphi components:
	- a) TXYGraph: a component for xy-diagrams from Grahame Grieve at [Kestral Com](http://www.kestral.com.au)[puting](http://www.kestral.com.au)
	- b) RZNEdit: an advanced edit field component from [Robert Kratz](mailto:kratz@labs.polycnrs-gre.fr)
	- c) TParser 10.1: a function parsing component from [Stefan Hoffmeister](mailto:Stefan.Hoffmeister@Uni-Passau.de) based on previous work of [Renate Schaaf](mailto:schaaf@math.usu.edu) and [Alin Flaider](mailto:aflaidar@datalog.ro)
	- d) TGotoWeb: a browser launching component by [Sylvain Cresto](mailto:Cret@mygale.org)
	- e) TVersionInfo: a non-visual component that reads the version information of a file, by an unknown author

All of them are freeware and can be found on the [Delphi Super Page](http://sunsite.icm.edu.pl/delphi/).

# <span id="page-27-0"></span>6 Appendix

# Acknowledgements

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